

MATH FIELD DAY 2003 - Relay A

A1 Given a right triangle with a hypotenuse of 3 and one leg of $2\sqrt{2}$, find the length of the other leg.

A2 Let $k =$ the number you receive.

Find the value of
$$\frac{1}{1 + \frac{1}{1 + \frac{1}{k}}}$$

A3 Let $k =$ the number you receive.

Solve for x : $2 = \frac{k(k+x)}{2}$

A4 Let $k =$ the number you receive.

If $f(x-1) = 3x - 4$, find $f(k)$.

A5 Let $k =$ the number you receive.

Find A if $p(x) = x^2 + kx + A$
and one zero of $p(x)$ is 4 times the other.

1

$\frac{2}{3}$

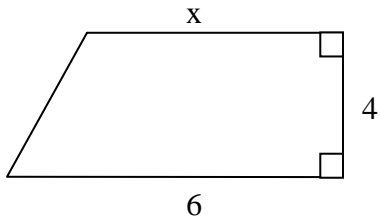
$\frac{16}{3}$

15

36

MATH FIELD DAY 2003 - Relay B

- B1 The top and bottom are perpendicular to the right edge.
The figure has area 16. What is x ?



- B2 Let $k =$ the number you receive. What is the remainder when $x^3 - x^2 + 4$ is divided by $x - k$?

- B3 Let $k =$ the number you receive. The line $y = -kx + k$ forms a triangle with the lines $x = 0$ and $y = 0$. What is the area of the triangle?

- B4 Let $k =$ the number you receive. How many quarts of water must be added to k quarts of antifreeze to give a solution that is 80% antifreeze?

- B5 Let $k =$ the number you receive. If $\tan \theta = k$, evaluate $\sin^2 \theta$.

2

8

4

1

1/2

MATH FIELD DAY 2003 - Relay C

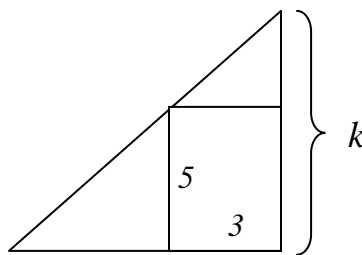
C1 How many ways are there to choose two students to get A's out of a seminar with four students?

C2 Let $k =$ the number you receive. If $2^k x = y$, $x^5 y = 8^k$, and $x = 2^r$, what is r ?

C3 Let $k =$ the number you receive. If $(k + \sqrt{2})^3 = a + b\sqrt{2}$ for integers a and b , what is b ?

C4 Let $k =$ the number you receive. Find the y -coordinate of the vertex of the parabola $y = x^2 + kx + 55$.

C5 Let $k =$ the number you receive. A rectangle of base 3 and height 5 is inscribed in a right triangle of height k . How long is the base of the triangle?



6

2

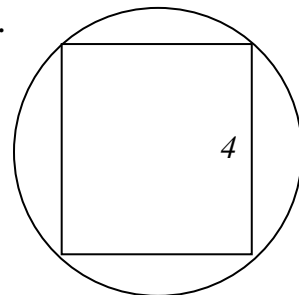
14

6

18

MATH FIELD DAY 2003 - Relay D

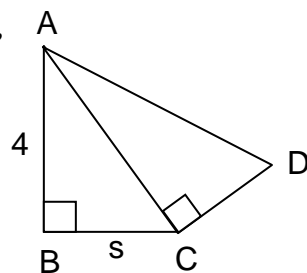
D1 A rectangle of height 4 is inscribed in a circle of area 5π .
How long is the base of the rectangle?



D2 Let $k =$ the number you receive.

If $x = k + \frac{2k^2}{x}$ and $x > 0$, what is x ?

D3 Let $s =$ the number you receive from the person in front of you,
and $t =$ the number you receive from the person behind you.
If $\angle ABC = 90^\circ = \angle ACD$, $BC = s$, and $CD = t$, find AD .



D4 Let $k =$ the number you receive.

What is the radius of the circle $x^2 + y^2 - 8y + k = 0$?

D5 How many ways are there to arrange the letters in MEMO?

