

MATH FIELD DAY 2005 RELAYS

Relay A

- A1. Find the slope of the line with equation $6x - 2y = 3$.
- A2. Let k be the number you receive. Find the sum of the positive integer factors of $2k$, including 1 and $2k$.
- A3. Let k be the number you receive. Find the y coordinate of the point of intersection of the lines with equations $x + 3y = 6k$ and $x - y = 2k$.
- A4. Let k be the number you receive. Lines from the center of a regular polygon to the vertices divide the polygon into k congruent triangles. What number is the degree measure of the smallest angle of each triangle?
- A5. Let k be the number you receive. Find the largest solution of the equation $x^2 - 7x = k$.

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Relay B

B1. Find the degree of the polynomial $\left(\frac{1}{2}x - 2\right)^2 \cdot (2x + 3)^4$.

B2. Let k be the number you receive. What negative number satisfies the equation $x^2 - kx = 16$?

B3. Let k be the number you receive. How many positive prime numbers are less than $10 - k$? (Remember that 1 is NOT a prime.)

B4. Let k be the number you receive. Find the slope of the line with equation $3x + ky = k^2$.

B5. Let k be the number you receive. Find $\frac{3k - 1}{k + 1}$.

1. 6

2. -2

3. 5

4. -3/5

5. $\textcircled{-7}$

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Relay C

C1. Find the positive integer k such that $(k + 1)^2$ and k^2 differ by 13.

C2. Let k be the number you receive. Find the radius of the circle with circumference πk .

C3. Let k be the number you receive. Find the real root of $x^3 - 9k = 0$.

C4. Let k be the number you receive. Find the area of the right triangle with legs of lengths k and 6 and hypotenuse $\sqrt{36 + k^2}$.

C5. Let k be the number you receive. Find the number of distinct positive integer factors of k^2 .

1. 6

2. 3

3. 3

4. 9

5. 5

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Relay D

D1. Find the solution of the equation $\frac{2^{x-1}}{8} = 4$.

D2. Let k be the number you receive. Find the solution of the equation $\frac{5x+3}{x-1} = k$.

D3. Let k and h be the numbers you receive. If k and h are the roots of the polynomial $x^2 + bx + c$, find b .

D4. Let h be the number you receive. Find the x -intercept of the line with equation $6x + 2y = h^2$.

D5. Find the smallest positive number k that has four different positive factors: 1, k , and two other integers.

1. 6

2. 9

3. **-15**

4. 6

5. 6